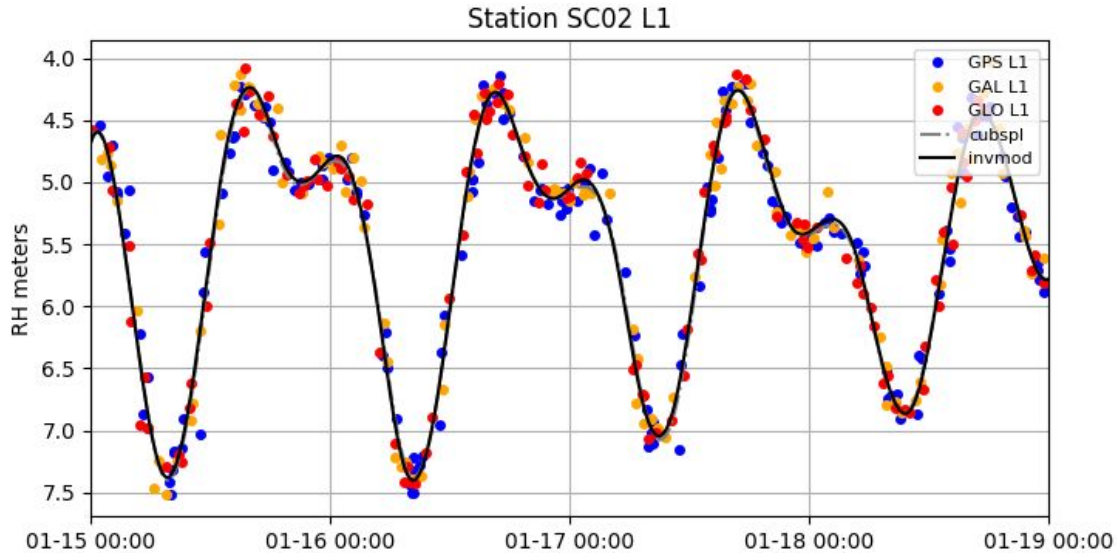


# 2023 GNSS-IR short course: 'invsnr'



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# What is 'invsnr'?

'invsnr' is a physics-informed way of obtaining a smoothly varying reflector height / water level time series at regular intervals

Why is it useful?

- Water levels tend to vary smoothly
- Satellite passes are randomly distributed in time
- Difficult to interpret data points from the same time with different values
- Smoothing reduces the effect of random noise in spectral analysis

When is it useful?

- If you care about sub-daily reflector heights e.g., tides, flooding
- If your signal is smaller or similar magnitude to random noise in measurements

# History of 'invsnr'

 AGU PUBLICATIONS



## Radio Science

### RESEARCH ARTICLE

10.1002/2016RS006057

#### Key Points:

- We present an advanced method for retrieving sea surface heights using

## Improving GNSS-R sea level determination through inverse modeling of SNR data

Joakim Strandberg<sup>1</sup>, Thomas Hobiger<sup>1</sup>, and Rüdiger Haas<sup>1</sup>

## Quantifying the Uncertainty in Ground-Based GNSS-Reflectometry Sea Level Measurements

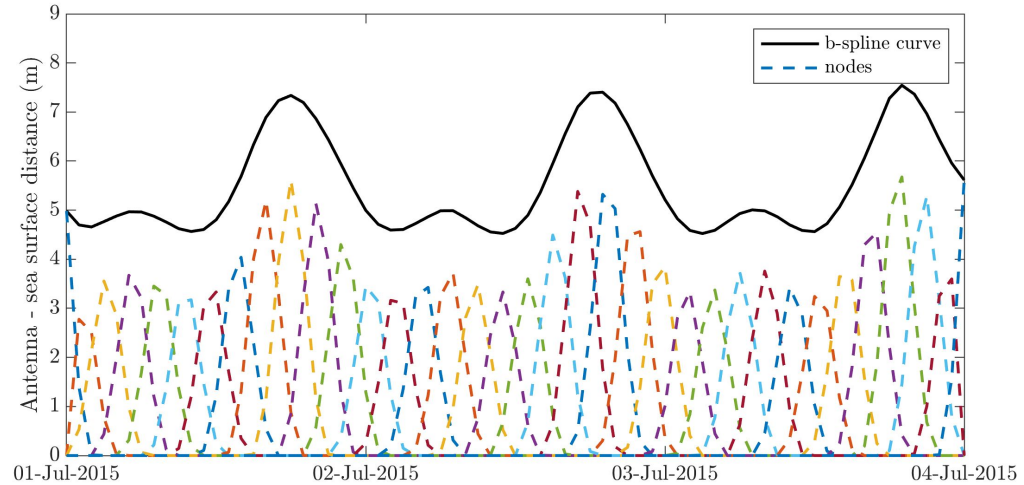
David Purnell<sup>1</sup>, Natalya Gomez<sup>1</sup>, Ngai Ham Chan<sup>1</sup>, Joakim Strandberg<sup>1</sup>, David M. Holland<sup>1</sup>, and Thomas Hobiger<sup>1</sup>

## Precise water level measurements using low-cost GNSS antenna arrays

David J. Purnell<sup>1</sup>, Natalya Gomez<sup>1</sup>, William Minarik<sup>1</sup>, David Porter<sup>2</sup>, and Gregory Langston<sup>1</sup>

# From Strandberg et al. (2016)

- Reflector heights (Water levels) are modeled using a b-spline curve
- The curve is defined by node values with e.g., 12 nodes per 24hr
- Water level measurements can be taken at any time on the curve

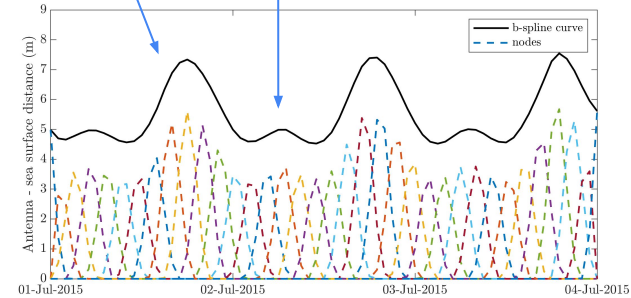
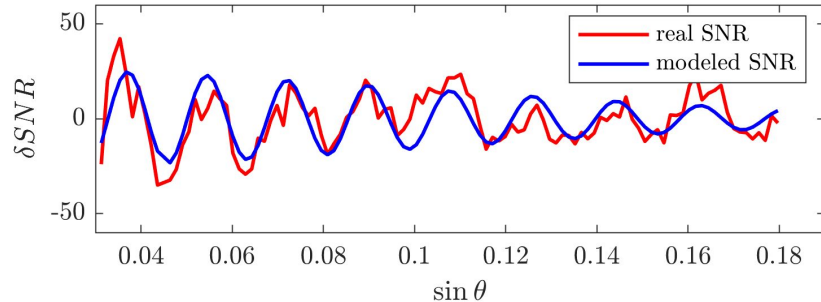


# From Strandberg et al. (2016)

- SNR data is modeled using:
- Inverse method: if real and modeled SNR match, then reflector height model should be good

$$\delta\text{SNR} = \left( C_1 \sin\left(\frac{4\pi h}{\lambda} x\right) + C_2 \cos\left(\frac{4\pi h}{\lambda} x\right) \right) e^{-4k^2 \Lambda x^2}$$

related to antenna gain pattern, surface roughness...



# Improvements

- Node values are first estimated using spectral analysis reflector height estimates (including 'rhdot' correction)
- Simplified spline curve:
  - Regularly spaced nodes (points along curve)
  - Cubic spline interpolation between points

Dominant peak  
from spectral  
analysis

dh/dt taken from  
curve

$$f = \frac{2}{\lambda} \left[ h + \frac{\partial h}{\partial t} \frac{\tan \theta}{\partial \theta / \partial t} \right]$$

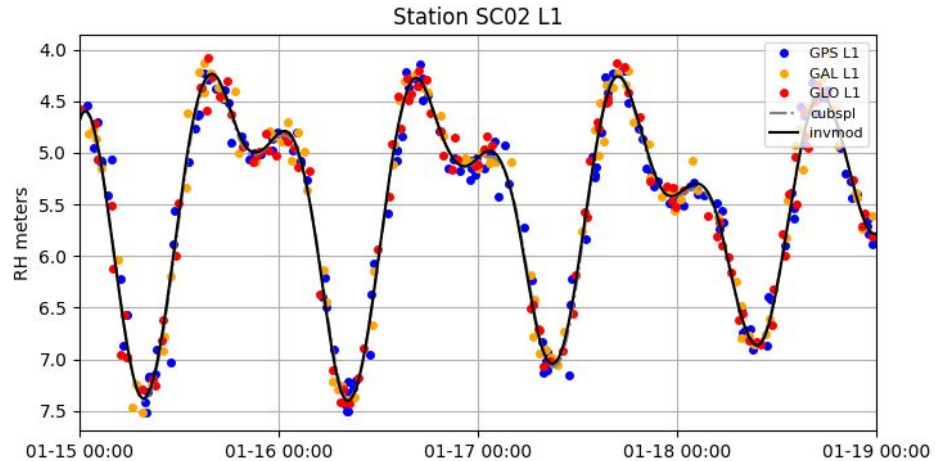
## Example: SC02, Friday Harbor, WA

```
rinex2snr sc02 2021 015 -orb gnss -doy_end 045
```

```
invsnr_input sc02 3 12 5 13 -a1 60 -a2 240
```

```
invsnr sc02 2021 015 L1 -doy_end 018 -pktlim 6
```

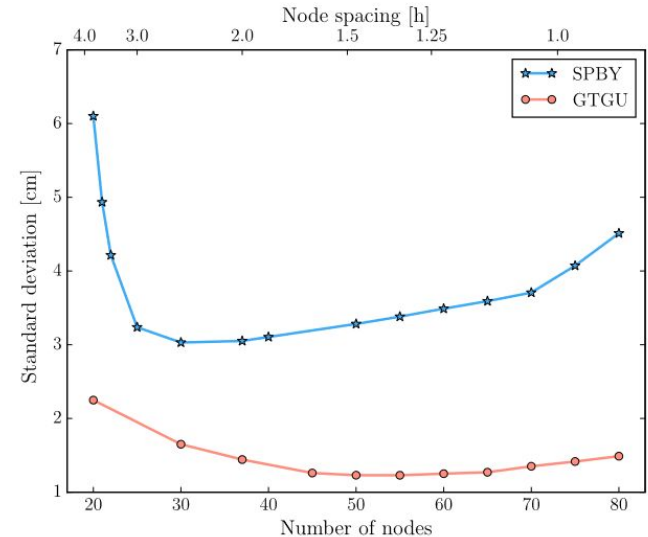
- Azimuth (a1, a2), elevation angle and reflector height limits taken from literature
- More important to get multiple constellations than multiple frequencies, hence '-orb gnss' and 'L1'



## Note on parameters: 'knot\_space' and 'risky'

- The time between nodes is set using 'knot\_space' (in hours)
- The more frequent the nodes, the more accurate water level representation is theoretically possible
- However, if there is a gap in the data bigger than the node spacing, there might be instabilities (unphysical height variations)

**Note: this is the same problem as 'overfitting' in machine learning**



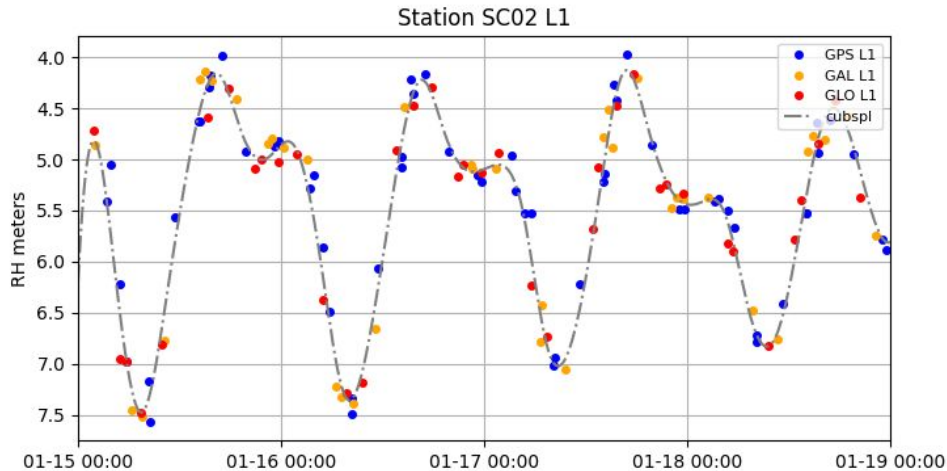
From Strandberg et al. (2016)



## Note on parameters: 'knot\_space' and 'risky'

```
invsnr_input sc02 3 12 5 13 -a1 60 -a2 120
```

```
invsnr sc02 2021 015 L1 -doy_end 018 -snrfit False
```

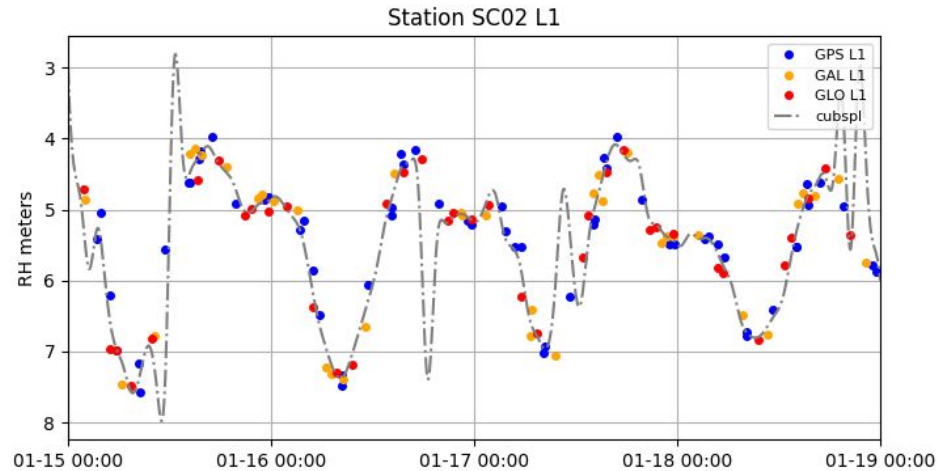


Default  
knot\_space = 3

# Note on parameters: 'knot\_space' and 'risky'

```
invsnr_input sc02 3 12 5 13 -a1 60 -a2 120
```

```
invsnr sc02 2021 015 L1 -doy_end 018 -snrfit False -risky True -knot_space  
1
```

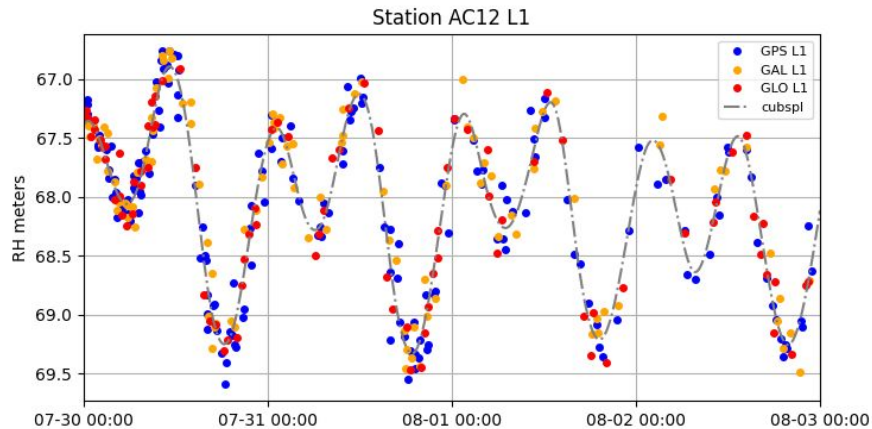


## Example 2: AC12, Chernabura, AK

```
rinx2snr ac12 2022 211 -doy_end 214 -orb gnss -rate high -archive unavco -dec 5
```

```
invsnr_input ac12 60 80 5 10
```

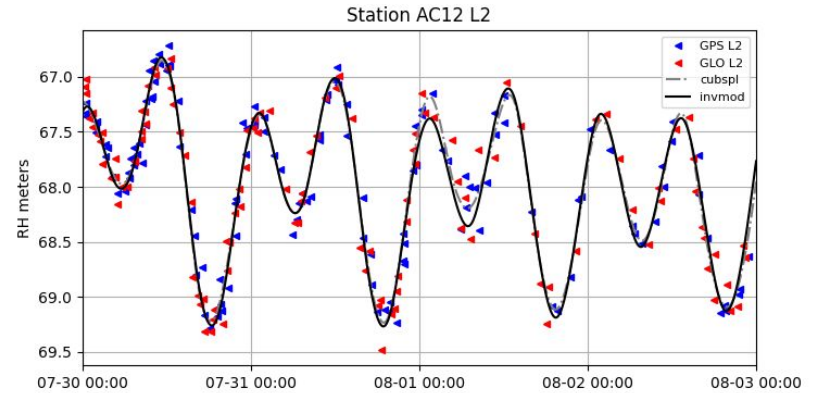
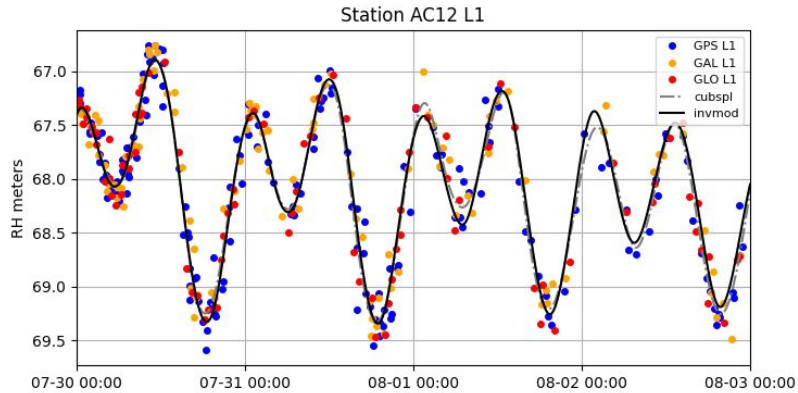
```
invsnr ac12 2022 211 L1 -doy_end 214 -snrfit False -pktnlim 9
```



## Example 2: AC12, Chernabura, AK

```
invsnr ac12 2022 211 L1 -doy_end 214 -pktlim 9
```

```
invsnr ac12 2022 211 L2 -doy_end 214 -pktlim 9
```



# Notes & tips

- Don't bother using 'invsnr' if the reflector heights don't look good to begin with!
  - Always start with 'quicklook' or refl zones web app
  - It is very important to have good azimuth and elevation angle masks
- If daily averages are good enough for your application, stick with that!
- If you are installing your own site and you want to use this technique the most important things are:
  - Wide view (azimuth) of surface
  - Multi-constellation data (just GPS is probably not good enough)
- Changing the input value 'roughness' might improve efficiency

If you want to improve the code:

- Better QC options
- Better SNR model (e.g., mpsim by Felipe & Kristine)
- Refraction correction: see work from Thalia Nikolaidou and co-authors